# 7.1.0 ENGINEERING MATHEMATICS I

### 7.1.1 Introduction

This module unit is designed to equip the trainee with the relevant mathematical knowledge, skills, techniques and attitudes necessary to enhance better understanding of other analytical units of this course, and at the same time provide the trainee with a firm foundation for further training in the trade.

## 7.1.2 General Objectives

By the end of this module unit, the trainee should be able to:

- a) use mathematical concepts and techniques in solving problems related to Mechanical Engineering trade
- b) organize, draw simple deductions and conclusions from the given data
- c) interpret graphical representation of functions relevant to the Mechanical Engineering trade area.

## 7.1.3 Module Unit Summary and Time Allocation

	MATICST		
Code	Sub module unit	0.1	Time
7.1.01	Fractions and Decimals	<ul> <li>Proper fractions and mixed numbers</li> <li>Conversion of mixed and improper Fractions and vice versa</li> <li>Application of the knowledge of decimals to engineering problems</li> <li>Application of fraction to real life situations</li> <li>Conversion of fractions into decimals and vice versa</li> <li>Recurring decimals/fractions</li> <li>Compare fractions</li> </ul>	14
7.1.02	Indices and Logarithms	<ul> <li>Base and index</li> <li>Laws of indices</li> <li>Indicial equations 'logarithm</li> <li>Laws of logarithm</li> <li>Logarithmic equations</li> <li>Conversion of bases</li> <li>Use of calculator</li> </ul>	10

## MATHEMATICS I

Code	Sub module unit		Time
7.1.03	Algebra	<ul> <li>Reduction of equations</li> <li>Solution of equations reduced to quadratic form</li> <li>Solutions of simultaneous linear equations in three unknowns</li> <li>Solution of problems involving AP and GP</li> </ul>	14
7.1.04	Trigonometry	<ul> <li>Half –angle formula</li> <li>Factor formula</li> <li>Trigonometric functions</li> <li>Parametric equations</li> </ul>	10
7.1.05	Permutations and Combinations	<ul> <li>Definition of permutation</li> <li>Definition of combination</li> <li>The factaral notation</li> <li>Expressions involving permutations and combinations</li> <li>Solution of problems involving permutations and combinations</li> </ul>	12
7.1.06	Binomial Expansion	<ul> <li>Binomial theorem Power series using binomial theorem Roots of numbers using binomial theorem</li> <li>Estimation of errors of small changes using binomial theorem</li> </ul>	12
7.1.07	Coordinate Geometry	<ul> <li>Polar equations</li> <li>Cartesian equation</li> <li>Graphs of polar equations</li> <li>Normals and tangents</li> </ul>	12
7.1.08	Hyperbolic Functions	<ul> <li>Definition of hyperbolic equations</li> <li>Properties of hyperbolic functions</li> <li>Evaluation of hyperbolic functions</li> <li>Hyperbolic identities</li> <li>Osborne's Rule</li> <li>ashx+bshx=C equation</li> </ul>	18

Code	Sub module unit		Time
7.1.09	Inverse Functions	<ul> <li>One to-one relationship in functions</li> <li>Inverse functions for one-to- one relationship</li> <li>Inverse functions for trigonometric functions</li> <li>Graph of inverse functions</li> <li>Inverse hyperbolic functions</li> </ul>	18
7.1.10	Complex numbers	<ul> <li>Definition of complex numbers</li> <li>Stating complex numbers in terms of conjugate argument and</li> <li>modulus</li> <li>Representation of complex numbers on the Argand diagram</li> <li>Arithmetic operation of complex numbers</li> <li>Application of Demoivre's theorem</li> <li>Application of complex numbers to engineering</li> </ul>	12
Total Ti	me 🤝	· · · · · · · · · · · · · · · · · · ·	132

# 7.1.01 FRACTIONS AND DECIMALS

7.1.01T0 Specific Objectives By the end of the sub module unit, the trainee should be able to:

> a) identify proper, improper and mixed fractions

b) convert mixed numbers to improper fractions and vice versa

- c) compare fractions
- d) apply the knowledge of fractions to real life situations

e) convert fractions into decimals and vice versa

- f) identify recurring decimals
- g) convert recurring decimals into fractions

 h) apply the knowledge of decimals to engineering problems

## 7.1.01C Competence

The trainee should have the ability to:

- i) perform the basic operations on fraction and decimals
- ii) apply the knowledge of

fractions and
decimals in
engineering

### Content

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7.1.01T1	Proper fractions and
	mixed numbers
7.1.01T2	Conversion of mixed
	and improper
	fractions and vice
	versa
7.1.01T3	Compare fractions
7.1.01T4	Application of
	fraction to real life
	situations
7.1.01T5	Conversion of
	fractions into
~	decimals and vice
A.	versa
7.1.01T 6	Recurring decimals
7.1.01T 7	Conversion of
	recurring decimals
	into fractions
7.1.01T 8	Application of the
	knowledge of
	decimals to
	engineering problems
	Suggested Learning
	Resources
	- Chart illustration
	on fractions
	equivalent
	fraction
	machon

- Real life situations

## 7.1.02 INDICES AND LOGARITHMS

7.1.02T1 Specific Objectives By the end of the sub module unit, the trainee should be able to:

- a) define the terms base and index
- b) state the laws of indices
- c) perform simple operations of indices
- d) define the term logarithm
- e) state laws of logarithms
- f) perform simple operations of logarithms
- g) change the bases of logarithms
- h) Use calculator in solving problems related to logarithms
- 7.1.02C Competence The trainee should have the ability to work out mathematical problems related to indices and logarithms

#### Content

- 7.1.02T 1 Base and index
  7.1.02T 2 Laws of indices
  7.1.02T 3 Simple operations on d) indices
  7.1.02T 4 Indicial equations 'logarithm
  7.1.02T 5 Laws of logarithm
  7.1.02T 6 Logarithmic equations
- 7.1.02T 7 Conversion of bases

7.1.02T 8 Use of calculator in solving problems related to logarithms

Suggested Learning Resources

- Calculates
- Charts
- Audio visual media

# 7.1.03 ALGEBRA

7.1.03T1 Specific Objectives By the end of the sub module unit, the trainee should be able to: reduce logarithmic

equations to quadratic equations

- a) solve equations reduced to quadratic forms
- b) solve linear simultaneous equations with three unknowns
- c) solve problems involving arithmetic progression and geometric progression
- 7.1.03C Competence
   The trainee should have
   the ability to solve
   problems involving
   arithmetic progression
   and geometric
   progression
   Content

   7.1.03T1 Reduction of

equations

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7.1.03T2	Solution of equations
	reduced to quadratic
	form

- 7.1.03T3 Solutions of simultaneous linear equations in three unknowns
- 7.1.03T4 Solution of problems involving AP and GP

Suggested Learning Resources

- Print media
- Audio media
- Real live experience

#### 7.1.04T0 TRIGONOMETRY

7.1.04T0 *Specific Objectives* By the end of the sub module unit, the trainee should be able to:

- a) Derive the halfangle
- b) Derive the factor formula
- c) Solve trigonometric functions
- d) Determine parametric equations
- 7.1.04C *Competence* The trainee should have the ability to solve problems in trigonometry

	Content		
7.1.04T1	Half –angle formula		
7.1.04T2	Factor formula		

7.1.04T3 Trigonometric functions
7.1.04T4 Parametric equations

#### Suggested Learning Resources

- Charts
- Mathematical tables
- Calculators
- Light-angled triangles
- Real life experience

PERMUTATIONS AND COMBINATIONS

7.1.05

7.1.05T0

Specific Objectives By the end of the sub module unit, the trainee should be able to:

- a) define the term permutation
- b) define the term combination
- c) express numbers in factorial notation
- d) simplify expressions involving permutations and combinations
- e) solve problems involving permutation and combination.

7.1.05C *Competence* The trainee should have the ability to solve problems in

	permutations and combinations	7.1.06C	<i>Competence</i> The trainee should have
	Content		the ability to apply
7.1.05T1	Definition of		binomial theorem to
	permutation		estimating errors
7.1.05T2	Definition of		
7 1 05772	combination The factorial notation	7 1 0471	<i>Content</i> Binomial theorem
7.1.05T3 7.1.05T4	Expressions involving	7.1.06T1 7.1.06T2	Power series using
7.1.0314	permutations and	7.1.0012	binomial theorem
	combinations	7.1.06T3	Roots of numbers
7.1.05T5	Solution of problems	/////010	using binomial
	involving		theorem
	permutations and	7.1.06T4	Estimation of errors
	combinations		of small changes
			using binomial
	Suggested Learning		theorem
	Resources	$\sim$	G . 17 .
	- Charts	-01	Suggested Learning
	- Real life situations	6	<i>Resources</i> - Charts
7106	<b>DINOMIAI</b>	<u>,                                    </u>	- Charts
7.1.06		7.1.07	
7.1.06	BINOMIAL EXPANSION	7.1.07	- Charts COORDINATE GEOMETRY
<b>7.1.06</b> 7.1.06T0	EXPANSION		COORDINATE
			COORDINATE
	EXPANSION Specific Objectives	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub
	EXPANSION Specific Objectives By the end of the sub	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to:	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial	7.1.07	<b>COORDINATE</b> <b>GEOMETRY</b> <i>Specific Objectives</i> By the end of the sub module unit, the trainee should be able to:
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial theorem	7.1.07	<b>COORDINATE</b> <b>GEOMETRY</b> <i>Specific Objectives</i> By the end of the sub module unit, the trainee should be able to: a) convert polar
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial theorem b) apply the binomial	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be able to: a) convert polar equations to
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial theorem b) apply the binomial theorem in deriving	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be able to: a) convert polar equations to cartesian equation
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial theorem b) apply the binomial theorem in deriving power series of	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be able to: a) convert polar equations to cartesian equation b) convert cartesian
	<ul> <li>EXPANSION</li> <li>Specific Objectives</li> <li>By the end of the sub module unit, the trainee should be able to:</li> <li>a) state the binomial theorem</li> <li>b) apply the binomial theorem in deriving power series of simple functions</li> </ul>	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be able to: a) convert polar equations to cartesian equation b) convert cartesian equation to polar
	EXPANSION Specific Objectives By the end of the sub module unit, the trainee should be able to: a) state the binomial theorem b) apply the binomial theorem in deriving power series of	7.1.07	COORDINATE GEOMETRY Specific Objectives By the end of the sub module unit, the trainee should be able to: a) convert polar equations to cartesian equation b) convert cartesian
	<ul> <li>EXPANSION</li> <li>Specific Objectives</li> <li>By the end of the sub module unit, the trainee should be able to:</li> <li>a) state the binomial theorem</li> <li>b) apply the binomial theorem in deriving power series of simple functions</li> <li>c) apply binomial</li> </ul>	7.1.07	<ul> <li>COORDINATE GEOMETRY</li> <li>Specific Objectives</li> <li>By the end of the sub module unit, the trainee should be able to: <ul> <li>a) convert polar</li> <li>equations to</li> <li>cartesian equation</li> </ul> </li> <li>b) convert cartesian</li> <li>equation to polar</li> <li>equations</li> <li>c) plot graphs of polar</li> <li>equations</li> </ul>
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7.1.07C	<i>Competence</i> The trainee should		e) sate the osborne's rule
	have the ability to		f) solve equations of
	work out problems in coordinat		the form aChx+bShx= c
	geometry		aCIIX+0SIIX=c
	geometry	7.1.08C	Competence
	Content	7.1.000	The trainee should have
7.1.07T1	Polar equations		the ability to work out
7.1.07T2	Cartesian equation		problems in hyperbolic
7.1.07T3	Graphs of polar		functions
	equations		
7.1.07T4	Normals and		Content
	tangents	7.1.08T1	Definition of
	-		hyperbolic equations
	Suggested	7.1.08T2	Properties of
	Learning		hyperbolic functions
	Resources	7.1.08T3	Evaluation of
	- Charts	$\sim$	hyperbolic functions
	- Squared grid-	7.1.08T4	Hyperbolic identities
	board	7.1.08T5	Osborne's Rule
	- Calculators	<b>7.1.08T6</b>	aChx+bshx=c
	x		equation
7.1.08	HYPERBOLIC		
	FUNCTIONS		Suggested Learning
	<b>0</b> ~		Resources
7.1.08T0	Specific Objectives		- Tables
	By the end of the sub		- Calculators
	module unit, the	<b>F</b> 1 00	
	trainee should be able	7.1.09	INVERSE FUNCTIONS
	to:		FUNCTIONS
	a) define hyperbolic functions	7.1.09T1	Specific Objectives
	b) deduce properties	/.1.0711	By the end of the sub
	of hyperbolic		module unit, the
	functions		trainee should be able
	c) evaluate hyperbolic		to:
	c) cvaruate hyperbolic		

- a) identify one-to-one relation in functions
  - b) define inverse function for trigonometric functions

functions for given

arguments

d) verify simple

hyperbolic

relationships of identities

	c) draws graphs of		By the end of the sub
	inverse functions		module unit, the
	d) describe many		trainee should be able
	valued nature of		to:
	functions		a) define a complex
	e) describe the		number
	principal of inverse		b) state complex
	trigonometric		numbers in three
	function		forms
	f) derive the inverse		c) segment complex
	hyperbolic function		numbers on the
	• •		argand diagram
7.1.08C	Competence		d) perform arithmetic
	The trainee should have		operation on
	the ability to work out		complex numbers
	problems in inverse		e) state and apply the
	functions		de moivre's
			theorem
	Content	~	f) apply complex
7.1.09T1	One to-one		numbers to
	relationship in	eQ.	engineering
	functions	$\mathfrak{X}^{\sim}$	problems
7.1.09T2	Inverse functions for	at.com	•
	one-to-one	7.1.10C	Competence
	relationship		The trainee should
7.1.09T3	Graph of inverse		have the ability to:
	functions		i) Demonstrations
7.1.09T4	Many valued nature		ii) Questions and
	of functions		answers
7.1.09T5	Principle of inverse		iii)Discussions
	trigonometric		
	function		Content
7.1.09T5	Inverse hyperbolic	7.1.10T1	Definition of complex
	functions		numbers
		7.1.10T2	Stating complex
	Suggested Learning		numbers in terms of
	Resources		conjugate argument
	- Tables		and modulus
	- Calculators	7.1.10T3	Representation of
			complex numbers on
7.1.10	COMPLEX		the Argand diagram
	NUMBERS	7.1.10T4	Arithmetic operation
			of complex numbers
7.1.10T0	Specific Objectives		

# 82

- 7.1.10T5 Application of De Moivre's theorem
- 7.1.10T6 Application of complex numbers to engineering problems

Suggested Learning Resources

- Charts
- Calculators

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